

## What is Spectroscopy?

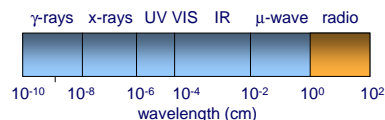
- Spectroscopy is the study of the interactions between **light** and **matter**.
- Here **light** refers to any sort of electromagnetic radiation, such as visible light, UV, IR, and radio waves.
- Depending on the **frequency** or **wavelength** of the radiation involved we will have different types of interactions with matter (molecules).

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## What is Spectroscopy?

- The following chart shows the ranges (wavelengths), for different types of spectroscopies.



- As you know, wavelength and frequency are inversely proportional, so higher frequencies mean shorter wavelength.

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## NMR Spectroscopy

### NMR

### NUCLEAR MAGNETIC RESONANCE

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## NMR Spectroscopy

### NUCLEAR MAGNETIC RESONANCE

- Some property of the nucleus is used
  - Should have net free spin
  - Spin Number  $I =$  Integral multiple of  $\frac{1}{2}$ 
    - $\pm 1/2, 3/2, 5/2, \dots$

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## NMR Spectroscopy

### NUCLEAR MAGNETIC RESONANCE

- Two Magnetic fields are generated
  - External magnet
    - Permanent Magnet
    - Electro Magnet
    - Superconducting Magnet
  - Nuclear spin generates dipoles
    - Nucleus behaves as tiny bar magnets

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## NMR Spectroscopy

### NUCLEAR MAGNETIC RESONANCE

- Matching of Frequency
  - Precisional Frequency
  - Applied Radiofrequency

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## Spin Resonance (Magnetic Resonance)

- **Spin resonance** is a physical phenomenon resulting from the intrinsic angular momentum associated with the spin of the nucleus or electron of an atom.
- **These are of two types**
  - Nuclear Magnetic resonance
  - Electron Spin Resonance
- **Nuclear magnetic resonance (NMR)** implies that the nuclei of the atoms are in resonance, while
- **Electron spin resonance (ESR)** deals with electrons.

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## NMR History

- 1937 **Rabi** predicts and observes nuclear magnetic resonance
- 1946 **Bloch, Purcell** first nuclear magnetic resonance of bulk sample
- 1953 **Overhauser** NOE (nuclear Overhauser effect)
- 1966 **Ernst, Anderson** Fourier transform NMR
- 1975 **Jeener, Ernst** 2D NMR
- 1985 **Wüthrich** first solution structure of a small protein (BPTI) from NOE derived distance restraints
- 1987 3D NMR +  $^{13}\text{C}$ ,  $^{15}\text{N}$  isotope labeling of recombinant proteins (resolution)
- 1990 pulsed field gradients (artifact suppression)
- 1996/7 new *long range* structural parameters:
  - **residual dipolar couplings** from partial alignment in liquid crystalline media
  - projection angle restraints from **cross-correlated relaxation**
- TROSY (molecular weight > 100 kDa)

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## NMR History

### Nobel prizes

- 1944 *Physics* Rabi (Columbia)
- 1952 *Physics* Bloch (Stanford), Purcell (Harvard)
- 1991 *Chemistry* Ernst (ETH)
- 2002 *Chemistry* Wüthrich (ETH)
- 2003 *Medicine* Lauterbur (University of Illinois in Urbana), Mansfield (University of Nottingham)

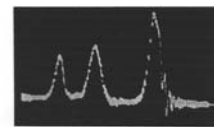
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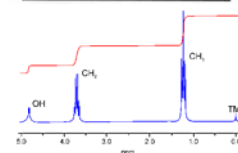
## NMR History

### First Observation of the Chemical Shift

#### $^1\text{H}$ NMR spectra ethanol



#### Modern ethanol spectra



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## Typical Applications of NMR

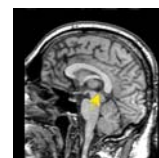
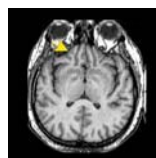
- 1.) Structural (chemical) elucidation
  - Natural product chemistry
  - Synthetic organic chemistry
    - analytical tool of choice of synthetic chemists
    - used in conjunction with MS and IR
- 2.) Study of dynamic processes
  - reaction kinetics
  - study of equilibrium (chemical or structural)
- 3.) Structural (three-dimensional) studies
  - Proteins, Protein-ligand complexes
  - DNA, RNA, Protein/DNA complexes
  - Polysaccharides
- 4.) Drug Design
  - Structure Activity Relationships by NMR
- 5.) Medicine -MRI

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## Typical Applications of NMR

- **MRI images of the Human Brain**



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## NMR Spectra

Each NMR Observable Nuclei Yields a Peak in the Spectra  
"fingerprint" of the structure

2-phenyl-1,3-dioxep-

<sup>1</sup>H NMR spectra

<sup>13</sup>C NMR spectra

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## Electro Magnetic Theory

### Basic Concept

A Direct Application to NMR

A moving perpendicular external magnetic field will induce an electric current in a closed loop

An electric current in a closed loop will create a perpendicular magnetic field

Magnetic field produced by circulating electron

Electromagnet

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## Electro Magnetic Theory

### Basic Concept

#### Faraday's Law of Induction

- If the magnetic flux ( $\Phi_B$ ) through an area bounded by a closed conducting loop changes with time, a current and an emf are produced in the loop. This process is called induction.
- The induced emf is:

$$\xi = -\frac{d\Phi_B}{dt}$$

Simple AC generator

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## Electro Magnetic Theory

### Basic Concept

#### Lenz's Law

- An induced current has a direction such that the magnetic field of the current opposes the change in the magnetic flux that produces the current.
- The induced emf has the same direction as the induced current

Direction of current follows motion of magnet

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## Concept of Spin

- Spin is a fundamental property of all elementary particles and is typically viewed as the intrinsic angular momentum.
- Both electrons and nuclei possess spin, and these spins precess around the direction defined by an applied magnetic field.
- The frequency of precession scales with the applied field and is roughly 1,000 times faster for electrons.

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## Concept of Spin

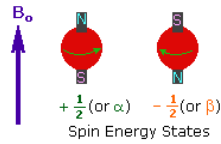
- A spinning charge generates a magnetic field, as shown by the animation on the right. The resulting spin-magnet has a magnetic moment ( $\mu$ ) proportional to the spin.

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## Concept of Spin

- 2. In the presence of an external magnetic field ( $B_0$ ), two spin states exist,  $+1/2$  and  $-1/2$ .

The magnetic moment of the lower energy  $+1/2$  state is aligned with the external field, but that of the higher energy  $-1/2$  spin state is opposed to the external field. Note that the arrow representing the external field points North.



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## The Gory Details

- Only nuclei with **spin number** ( $I \neq 0$ ) can absorb/emit electromagnetic radiation.
  - Even atomic mass & number  $\Rightarrow I = 0$  ( $^{12}\text{C}$ ,  $^{16}\text{O}$ )
  - Even atomic mass & odd number  $\Rightarrow I = \text{whole integer}$  ( $^{14}\text{N}$ ,  $^2\text{H}$ ,  $^{10}\text{B}$ )
  - Odd atomic mass  $\Rightarrow I = \text{half integer}$  ( $^1\text{H}$ ,  $^{13}\text{C}$ ,  $^{15}\text{N}$ ,  $^{31}\text{P}$ )
- The **spin states** of the nucleus ( $m$ ) are **quantized**:
 

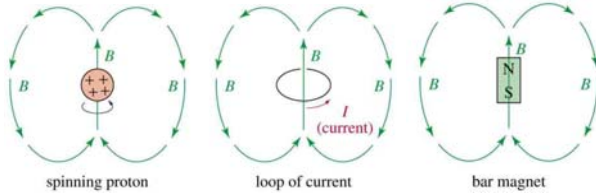
$m = I, (I - 1), (I - 2), \dots, -I$
- Properly,  $m$  is called the **magnetic quantum number**

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## Nuclear Spin

- A nucleus with an odd atomic number or an odd mass number has a nuclear spin.
- The spinning charged nucleus generates a magnetic field.

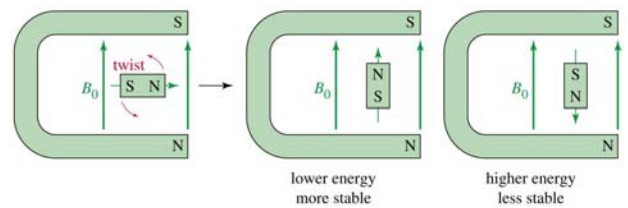


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## External Magnetic Field

When placed in an external field, spinning nuclei act like bar magnets.



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## Precession

- To explain everything in NMR we have to refer to rotation, and Hz are not the best units to do this. We define the **precession** or **Larmor** frequency,  $\omega_0$ , in radians:

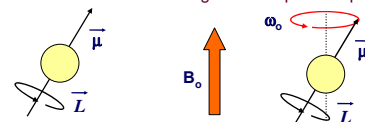
$$\omega_0 = 2\pi\nu_0 \Rightarrow \omega_0 = \gamma B_0 \text{ (radians)}$$

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## Precession

- With what precession is  $\omega_0$  related to? One thing we left out of the mix was the **angular momentum**,  $L$ , associated with all nuclei (magnetic or not).
- We can think of nuclei as small magnetized tops that spin on their axis



- After turning the magnet on we'll have two forces acting on the spins. One that tries to turn them towards  $B_0$ , and the other that wants to maintain their angular momentum. The net result is that the nuclei spins like a top

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## Theory of Magnetic Resonance

### Classical Description

- Spinning particle precesses around an applied magnetic field

A Spinning Gyroscope in a Gravity Field

Applied magnetic field

Precessional orbits

Spinning nucleus

$L = \hbar \sqrt{I(I+1)}$

$E = \text{rotational quantum number}$

$\mu = \frac{e}{2m} L$

$S$

$L$

$\mu$

$B_0$

## Theory of NMR

### Quantum Description

- Nuclear Spin (think electron spin)
  - Nucleus rotates about its axis (spin)
  - Nuclei with spin have angular momentum (p) or spin

1) total magnitude

$$\hbar \sqrt{I(I+1)}$$

1) quantized, spin quantum number I

2)  $2I + 1$  states:  $I, I-1, I-2, \dots, -I$

$I = 1/2$ :  $-1/2, 1/2$

3) identical energies in absence of external magnetic field

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## Magnetic Alignment

$\uparrow = \gamma h / 4\pi$

In the absence of external field, each nuclei is energetically degenerate

Add a strong external field ( $B_0$ ) and the nuclear magnetic moment: aligns with (low energy) against (high-energy)

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## Quantum Description

### Spins Orientation in a Magnetic Field (Energy Levels)

- Magnetic moment are no longer equivalent
- Magnetic moments are oriented in  $2I + 1$  directions in magnetic field

- Vector length is:  $\hbar \sqrt{I(I+1)}$
- Angle ( $\phi$ ) given by:  $\cos \phi = \frac{m}{\sqrt{I(I+1)}}$
- Energy given by:  $E = -\frac{m\mu}{I} B_0$

where,  $B_0$  - magnetic Field  
 $\mu$  - magnetic moment  
 $h$  - Planck's constant

For  $I = 1/2$

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## Quantum Description

### Net Magnetization

### Spins Orientation in a Magnetic Field (Energy Levels)

- Magnetic moments are oriented in one of two directions in magnetic field (for  $I = 1/2$ )

Difference in energy between the two states is given by:

$$\Delta E = \gamma h B_0 / 2\pi$$

where:  $B_0$  - external magnetic field  
 $h$  - Planck's constant  
 $\gamma$  - gyromagnetic ratio

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## Quantum Description

### Net Magnetization

### Spins Orientation in a Magnetic Field (Energy Levels)

- Transition from the low energy to high energy spin state occurs through an absorption of a photon of radio-frequency (RF) energy

Frequency of absorption:  $\nu = \gamma B_0 / 2\pi$

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## Quantum Description

### Net Magnetization

**NMR Signal (sensitivity)**

- The applied magnetic field causes an energy difference between the aligned ( $\alpha$ ) and unaligned ( $\beta$ ) nuclei
- NMR signal results from the transition of spins from the  $\alpha$  to  $\beta$  state
- Strength of the signal depends on the population difference between the  $\alpha$  and  $\beta$  spin states

Low energy gap  
 $\Delta E = h\nu$   
 $B_0 > 0$   
 $B_0 = 0$

- The population ( $N$ ) difference can be determined from the Boltzmann distribution and the energy separation between the  $\alpha$  and  $\beta$  spin states:

$$N_\alpha / N_\beta = e^{-\Delta E / kT}$$

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## Classical Description

### Net Magnetization

- Where does the net magnetization come from? In order to figure it out we translate all the spins to the origin of the coordinate system. We'll see something like this:

- We'll have a slight excess of spins aligned with  $B_0$ , but at any angle with respect to  $z$ . The distribution is proportional to  $N_\alpha / N_\beta$ .

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## Classical Description

### Net Magnetization

• If we decompose the  $m$  vectors in  $z$  and  $\langle xy \rangle$ , we get

The net magnetization *is* aligned with  $B_0$ , and this is what we use in NMR.

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## Classical Description

### Net Magnetization

- Nuclei either align with or against external magnetic field along the  $z$ -axis.
- Since more nuclei align with field, net magnetization ( $M_0, M_z$ ) exists parallel to external magnetic field.
  - Net Magnetization along  $+z$ , since higher population aligned with  $B_0$ .
  - Magnetization in  $X, Y$  plane ( $M_x, M_y$ ) averages to zero.

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## Net Magnetization

**Classic View:**

- Nuclei either align with or against external magnetic field along the  $z$ -axis.
- Since more nuclei align with field, net magnetization ( $M_0$ ) exists parallel to external magnetic field

**Quantum Description:**

- Nuclei either populate low energy ( $\alpha$ , aligned with field) or high energy ( $\beta$ , aligned against field)
- Net population in  $\alpha$  energy level.
- Absorption of radio-frequency promotes nuclear spins from  $\alpha \rightarrow \beta$ .

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## Resonance

### Absorption of RF Energy or NMR RF Pulse

**Classic View:**

- Apply a radio-frequency (RF) pulse along the  $y$ -axis
- RF pulse viewed as a second field ( $B_1$ ), that the net magnetization ( $M_0$ ) will precess about with an angular velocity of  $\omega_1$
- precession stops when  $B_1$  turned off

**Quantum Description:**

- enough RF energy has been absorbed, such that the population in  $\alpha/\beta$  are now equal
- No net magnetization along the  $z$ -axis

Please Note: A whole variety of pulse widths are possible, not quantized dealing with bulk magnetization

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